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A hierarchical model for eDNA fate and transport dynamics accommodating low concentration samples

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8 Abstract

9 Environmental DNA (eDNA) sampling is an increasingly important tool for answer-10 ing ecological questions and informing aquatic species management; however, 11 several factors currently limit the reliability of ecological inference from eDNA 12 sampling. Two particular challenges are (1) determining species source location(s) 13 and (2) accurately and precisely measuring low concentration eDNA samples in 14 the presence of multiple sources of ecological and measurement variability. The 15 recently introduced eDNA Integrating Transport and Hydrology (eDITH) model 16 provides a framework for relating eDNA measurements to source locations in riv-17 erine networks, but little empirical work has been done to test and refine model 18 assumptions or accommodate low concentration samples, that can be systematically 19 undermeasured. To better understand eDNA fate and transport dynamics and our 20 ability to reliably quantify low concentration samples, we developed a hierarchical 21 model and used it to evaluate a fate and transport experiment. Our model addresses 22 several low concentration challenges by modeling the number of copies in each PCR 23 replicate as a latent variable with a count distribution and conditioning detection 24 and quantification on replicate copy number. We provide evidence that the eDNA 25 removal rate declined through time, estimating that over 80% of eDNA was removed 26 over the first 10 m, traversed in 41 s. After this initial period of rapid decay, eDNA 27 decayed slowly with consistent detection through our farthest site 1 km from the 28 release location, traversed in 67.8 min. Our model further allowed us to detect extra-29 Poisson variation in the allocation of copies to replicates. We extended our hierar-30 chical model to accommodate a continuous effect of inhibitors and used our model 31 to provide evidence for the inhibitor hypothesis and explore the potential implica-32 tions. While our model is not a panacea for all challenges faced when quantifying 33 low-concentration eDNA samples, it provides a framework for a more complete 34 accounting of uncertainty.

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37 **1 Introduction**

Environmental DNA (eDNA) approaches are increasingly being used to estimate 38 ecological parameters like species distributions (Carraro et al. 2018), abundance 39 (Rourke et al. 2022), and phenology (Searcy et al. 2022) due to their detection sen-40 sitivity, wide applicability across species, and cost efficiency, among other reasons 41 (Jo and Yamanaka 2022). Further, eDNA sampling can be a particularly useful tool 42 for aquatic invasive species monitoring, potentially allowing for early detection and 43 eradication (Larson et al. 2020; Morisette et al. 2021; Sepulveda et al. 2020). How-44 ever, across many applications of eDNA monitoring in aquatic environments, the 45 reliability of ecological inference can be reduced by (1) uncertainty in the source 46 location of detected eDNA (Carraro et al. 2018; Jo and Yamanaka 2022) and (2) dif-47 ficulties measuring site and sample eDNA concentrations with minimal bias while 48 accounting for all relevant sources of uncertainty (Ellison et al. 2006; Shelton et al. 49 2019; Espe et al. 2022). Both of these factors have the potential to reduce the effec-50 tiveness of eDNA sampling for management action, depending on their magnitude 51 and how well they are addressed in experimental/monitoring design and statistical 52 analysis. 53

A key requirement for many aquatic applications of eDNA sampling, particularly 54 for invasive species monitoring, is to estimate source population locations because 55 the location where eDNA is detected is not necessarily where it was produced due 56 to hydrological transport (Carraro et al. 2018; Burian et al. 2021; Jo and Yamanaka 57 2022). In stream or river networks, eDNA flows downstream from the source(s) and 58 is detectable until the eDNA concentration attenuates below a detectable level due 59 to physical degradation (Lance et al. 2017) and/or removal from the water column 60 (Shogren et al. 2017). Therefore, an understanding of eDNA transport dynamics 61 is required to either localize source populations (e.g., Carraro et al. 2018) or more 62 broadly, estimate the plausible range of upstream distances a source population can 63 be located from a detection to direct next steps, like more intensive sampling for 64 confirmation (Sepulveda et al. 2023). 65

Environmental DNA fate and transport dynamics are the product of (1) eco-66 logical and biological factors determining how much eDNA is produced across 67 source populations (e.g., abundance, biomass, eDNA production rate), (2) hydro-68 logical factors (e.g., discharge, particle settling and resuspension, river network 69 connectivity), and (3) their interaction (e.g., eDNA degradation, removal from 70 water column to substrate) (Carraro et al. 2018; Curtis et al. 2021; Troth et al. 71 2021; Shogren et al. 2017). A recent modeling framework that includes these 72 general features is the eDNA Integrating Transport and Hydrology (eDITH) 73 model (Carraro et al. 2018, 2021), which has been used to predict the locations of 74 source populations and their eDNA production rates (Carraro et al. 2021) that can 75 correlate with abundance (Jo and Yamanaka 2022). The eDITH model is neces-76 sarily simplistic, given the number of factors that need to be accounted for with 77

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the typical level of eDNA sampling and the need to apply the model to large river networks which can be computationally intensive. Further, the eDITH model likelihood can be multimodal (described as "equifinality" by Carraro et al. 2021), with the eDNA removal rate parameter(s), the product of both physical decay and removal, being poorly estimated (Carraro et al. 2021). Therefore, prior information, particularly about the eDNA removal rate parameter(s), can improve parameter estimation and thus ecological inference (Carraro et al. 2021, 2023).

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Release experiments (e.g., Jane et al. 2015; Laporte et al. 2020,) have been 85 important for improving understanding of eDNA transport and removal dynam-86 ics, and they offer a means of providing parameter estimates that can be used as 87 prior information in future modeling when the source locations are not known in 88 advance (e.g., Carraro et al. 2018). Further, release experiments allow us to test 89 model assumptions (Bylemans et al. 2018; Yates et al. 2021), better evaluate the 90 level of realism necessary for reliable inference, and assess the data demands for 91 a given level of realism. For example, eDITH model applications to date have 92 assumed that the eDNA removal rate is constant with respect to time, which 93 could lead to biased estimates of source locations or detection distance from a 94 source if violated. In fact, the eDNA removal rate has been shown to decline with 95 time in some experiments (Bylemans et al. 2018; Yao et al. 2022; Snyder et al. 96 2023). Bylemans et al. (2018) hypothesized this decline may be due to variable 97 removal rates across eDNA fragments, such as between fragments in cells and 98 free-floating DNA, and Snyder et al. (2023) provided experimental evidence that 99 removal rate varies by particle size. To our knowledge, these hypotheses have 100 not been compared to empirical data within the eDITH framework, which is pos-101 sible in release experiments if the relevant hydrological variables are measured 102 accurately. 103

Another key requirement of many aquatic applications of eDNA sampling is 104 the accurate and precise quantification of eDNA concentration. While many eco-105 logical questions can be addressed with eDNA detection data alone (e.g., Hunter 106 et al. 2015), relating eDNA measurements to abundance or modeling eDNA produc-107 tion, transport, and removal as a function of hydrology require quantitative eDNA 108 measurements. These measurements can be obtained by quantitative or digital PCR 109 (Yates et al. 2019), where measurements are made across multiple PCR technical 110 replicates (hereafter 'replicates') of the same sample. These replicate-level measure-111 ments are typically then summarized and treated as data, usually using the mean 112 concentration across replicates as the sample concentration or averaging replicates 113 across samples to produce site concentrations (e.g., Yates et al. 2021). However, rep-114 licate measurements vary due to multiple factors including variable concentrations 115 across samples (Chambert et al. 2018; Shelton et al. 2019), variability in the allo-116 cation of eDNA copies to replicates (Rossmanith and Wagner 2011; Dorazio and 117 Hunter 2015; Tellinghuisen 2020), and measurement error in replicate copy number/ 118 concentration (Shelton et al. 2019; Espe et al. 2022). The common approach of aver-119 aging replicate concentrations does not partition multiple sources of variance and 120 pools the measurement error with the ecological variance, potentially eroding eco-121 logical inference if the measurement error is non-negligible in magnitude relative to 122 ecological variation. 123

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Low concentration samples present several unique challenges for accurate eDNA 124 quantification. First, eDNA copy number or concentration estimates are typically 125 modeled assuming approximate normality (usually on the log scale, see Carraro 126 et al. 2018; Espe et al. 2022), which is an accurate approximation at high concen-127 trations where copy numbers in replicates are large, but less so as concentrations 128 decline and there are few copies per replicate (Ellison et al. 2006; Dorazio and 129 Hunter 2015). Further, copy number measurements are often censored from below 130 by a fixed number of quantitative (q)PCR cycles or a limit of quantification or limit 131 of blank, which requires lower truncation of the observation model distribution 132 (Espe et al. 2022). Low concentration samples also present challenges for interpret-133 ing nondetections-as sample concentrations decline, both true negative (Poisson 134 sampling zeros) and false negative (failed detections) replicates become more likely, 135 which cannot be deterministically separated given the observed data (Ellison et al. 136 2006). In this situation, excluding zeros from sample means will introduce positive 137 bias, while including them may also introduce bias, with the direction depending 138 on the relative proportion of true and false negatives. Finally, sample concentra-139 tion can be underestimated due to interference by eDNA inhibitory compounds in 140 water samples (i.e., inhibition), which can be difficult to reliably detect (Kontanis 141 and Reed 2006; Lance and Guan 2020), and these inhibitors are more likely to affect 142 lower concentration samples (McKee et al. 2015; Hunter et al. 2019). Such under-143 estimation can bias ecological inference-for example, the eDNA removal rate in a 144 release experiment would be overestimated or the source location prediction from 145 an eDITH model would be too far away. These challenges for quantifying low con-146 centration samples are of particular concern when the goal is the early detection 147 of invasive species, which are easiest to eradicate when population sizes are small, 148 yet those populations produce less eDNA, yielding more samples where quantitative 149 measurements are unreliable. 150

Hierarchical models are useful for partitioning multiple sources of variation and 151 reducing bias by allowing the source(s) of bias to be modeled more mechanisti-152 cally (Royle and Dorazio 2008). These models are increasingly being used in eDNA 153 analyses-for example, multiscale occupancy models (Nichols et al. 2008; Dorazio 154 and Erickson 2018; Stratton et al. 2020) have been used to propagate uncertainty in 155 replicate-level occupancy states to site occupancy estimates and covariate relation-156 ships, and occupancy models have been extended to account for false positives (e.g., 157 Smith and Goldberg 2020; Guillera-Arroita et al. 2017). Hierarchical models have 158 been used for quantitative eDNA data to partition measurement and multiple levels 159 of environmental variation and relate both detection and quantitative measurements 160 to site concentration (Shelton et al. 2019; Espe et al. 2022). However, to deal with 161 the challenges of low concentration eDNA measurement, a hierarchical model rep-162 resenting the replicate copy numbers as latent discrete random variables may pro-163 vide improved inference. In such a model, the copy numbers can be assigned a more 164 appropriate count distribution, and the uncertainty in whether observed zeros are 165 true or false negatives can be propagated to the ecological parameters of interest. 166 Further, representing the copy numbers directly in the model may improve our abil-167 ity to assess lack of fit at the replicate level and investigate hypotheses about inhibi-168 tors affecting the replicate-level measurements. 169

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To better understand eDNA transport/removal, environmental variation, 170 measurement error, and our ability to jointly estimate the parameters of these 171 processes, we conducted an eDNA release experiment and developed a hier-172 archical model to apply to our experimental data that accommodates all three 173 sources of nondetections described above (no copies allocated to a replicate, 174 copies allocated but not detected, and copies allocated and detected, but meas-175 urement censored and treated as a nondetection). Of particular concern was how 176 well the eDITH model parameters are estimated and whether the eDNA removal 177 rate is constant or declining through time. Because we observed that our original 178 model did not adequately fit our experimental data, particularly for lower con-179 centration samples, we hypothesized that the source of poor fit could be eDNA 180 inhibitory compounds and expanded the model to accommodate the impact of 181 eDNA inhibitors on detection and copy number quantification. We used this 182 model to illustrate how inhibitors can bias inference of multiple parameters and 183 demonstrate how they can, in principle, be accommodated through hierarchical 184 modeling for more reliable ecological inference. 185

186 2 Field methods

187 2.1 DNA release

We conducted this experiment in the upper section of a 1st-order tributary of 188 the Gallatin River located on the Flying D Ranch in southwest Montana (USA), 189 2023 August 21–24. The upper section of this stream is approximately 1 m wide, 190 3-12 cm deep, a gradient of 50 m/km, had a mean discharge 0.02 (m³/s) dur-191 ing our study and flows into a small reservoir containing a conservation brood 192 stock of Arctic grayling (Thymallus arcticus), the target species for this study. 193 An artificial barrier restricts upstream movement of Arctic grayling from the 194 reservoir into the study reach-this species is absent in the watershed upstream 195 of the barrier. We introduced water collected from the reservoir's offshore zone 196 to the injection point (0 m) at the top of the 1000 m study reach; a plunge pool 197 occurred immediately downstream of the injection point and putatively helped 198 to mix introduced DNA. This experimental water was transported from the res-199 ervoir in ~ 200 L carboys and then transferred into bleached and rinsed coolers 200 connected in series and placed in a shaded area adjacent to the injection point. 201 The water was refreshed every 12 h. Beginning at time 0 h, water was dripped 202 into the stream at a rate of 220 mL/min for 49 h using an electric-operated 203 pump connected to the cooler series and 2.5-cm PVC that spanned the width 204 of the stream. Eight sprinkler emitters were attached to the PVC at 0.1 m inter-205 vals so that experimental water was dripped across the stream's width to facili-206 tate mixing. At time 32 h, eight Arctic grayling that were recreationally-angled 207 and legally harvested were added to the cooler series. Experimental water was 208 dripped into the stream until eDNA sampling concluded. 209

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210 2.2 eDNA sampling

211 2.5, 5, 10, 20, 40, 80, 125, 200, 300, 400, 500, 1000 m from the injection point. 212 Sampling was completed at all sites within 5 min. Buckets were bleached (50% 213 commercial bleach, Goldberg et al. 2016), rinsed with stream water upstream 214 of the injection point, and then repeatedly rinsed with stream water at the sam-215 pling point prior to collecting a sample. To collect samples, we filled the bucket 216 with stream water from the cross-section midpoint, swirled the bucket, and then 217 poured this water into each of six, 1-L sterile whirlpak bags. Our intention with 218 the buckets was to collect uniform samples at and across sampling points in as 219 short a time-increment as possible to minimize any temporal variability associ-220 ated with inconsistent eDNA production and removal rates. Bags were stored at 221 ambient temperatures in the shade and filtered on site through 47-mm diameter, 222 1.2 µm mixed cellulose ester filters (Millipore) within 90 min of collection. Fil-223 ters were placed immediately into 200 µL lysis buffer, which contained 20 µL of 224 proteinase K and 180 µL of Qiagen Buffer AE, and returned to USGS Northern 225 Rocky Mountain Science Center (NOROCK) for extraction and analysis. 226

We collected two field negative controls immediately before time 48 h, which consisted of 250-mL of deionized water poured into sterilized whirlpak bags. We collected field positive controls by sampling 1 L of water directly from the reservoir at time -24 and 0 h, and by sampling 1 L of water from the coolers at time 0, 24, and 48 h. Controls were handled similarly to experimental samples. Negative controls were filtered immediately prior to experimental samples, whereas positive controls were filtered at USGS NOROCK.

234 2.3 Hydrological covariates

Discharge was measured at all eDNA sample collection sites with the following 235 exceptions due to stream habitat complexity (e.g., undercut banks, large wood 236 and cobbles) that prevented accurate measurement: we used discharge measured 237 at 5 m for the first three sites at 0.5, 2.5 and 5 m; we used discharge measured 238 at 15 m for sites at 10 and 20 m; and we used discharge measured at 35 m for 239 the site at 40 m. Discharge measurements were estimated using the velocity-area 240 method (Herschy 1993), which involves dividing each site cross-section into mul-241 tiple subsections (approximately every 1 cm) and measuring the width, depth, 242 and flow velocity of each subsection with a hand-held current meter. Discharge 243 values for each subsection were summed to arrive at the cross-section discharge. 244 Discharge was sampled at time 24 h and time 49 h. We also deployed barometric 245 pressure transducers (Onset HOBO water level logger) set to 1-h intervals in the 246 air and water at 125 m to evaluate whether the water surface elevation (as a proxy 247 for discharge) was stable throughout our experiment. The transducer in the water 248 also collected water temperature at hourly increments. We deployed additional 249

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water temperature loggers (Onset HOBO pendant) at -0.5 and 1000 m to describe
water temperature at hourly increments.

252 3 Lab methods

253 3.1 Inhibition assessment

Here, we describe the methods to assess inhibition-all other lab methods are in 254 "Appendix". Inhibition was measured through the use of an exogenous internal posi-255 tive control (IPC) in every qPCR reaction, including controls (TaqManTM Exogenous 256 Internal Positive Control Reagents, cat. #4308321). We added 2 µL of VIC-labeled 257 10x Exo IPC Mix and 0.4 µL 50x Exo IPC DNA per qPCR reaction. Standard dilu-258 tions of IPC DNA were not used, so inhibition was assess using quantification cycle 259 (Cq) values determined from the methods described and referenced above. We used 260 ΔCq to describe inhibition of each qPCR reaction on a continuous scale: 261

$$\Delta Cq_{kp} = Cq_{kp} - \bar{C}q_{cp}, \tag{1}$$

where ΔCq_{kp} is the difference in IPC Cq_{kp} for qPCR reaction k on plate p and the mean Cq of a set of c uninhibited control samples on plate p ($\bar{C}q_{cp}$). Said another way, ΔCq_{kp} is the difference between a sample IPC Cq and the mean IPC Cq of a set of uninhibited samples on the same 96-well plate. Uninhibited control samples for each plate included no-template controls (NTCs) and synthetic standards with copy numbers of the target DNA strand < 1000. Positive values of ΔCq_{kp} reflect a delay in Cq, an indication of possible inhibiting effects.

271 **4 Modeling methods**

272 4.1 Data description

Our eDNA detection and quantification data are structured by site, sample, and PCR 273 replicate. Sites are numbered i = 1, ..., I = 13, each with a distance from the release 274 site, d_i , in sequential order starting at 0.5 m. At each site, samples are numbered 275 $j = 1, \dots, J = 6$, and for each sample, replicates are numbered $k = 1, \dots, K = 5$. We 276 define $y_{ij,k}^{obs}$ to be the measured copy number for site *i*, sample *j*, and replicate *k*, with 277 copy number measurements converted from the observed Cq values. Elements of 278 y^{obs} corresponding to failed detections are set to 0 as are any copy number observa-279 tions less than a lower bound for quantification, η^q . This quantification lower bound 280 can be set to the copy number corresponding to the maximum number of PCR 281 cycles used to account for data censoring due to a limited cycle number (Espe et al. 282 2022), or it can be set to exclude the lowest copy number measurements if (1) they 283 do not meet model assumptions (e.g., biased measurement at low concentrations, 284 discussed below), or (2) they are below a limit of blank and may be false positives 285 (Lesperance et al. 2021). 286

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Next, we define $y_{i,j,k}^{det}$ to be the detection data taking value 1 if the copy number 287 measurement is greater than η^d and 0 otherwise, where η^d is a lower bound of detec-288 tion that is less than or equal to the lower bound of quantification. For our analyses, 289 we set η^q to the copy number corresponding to 50 cycles and we set $\eta^d = 0$ because 290 we expect every sample to contain target eDNA. If false positives are a concern, 291 both η^d and η^q can be set higher, perhaps at the limit of blank (Lesperance et al. 292 2021). Note, these definitions of detection and quantification lower bounds differ 293 from standard definitions of "limit of detection" and "limit of quantification" (e.g., 294 Klymus et al. 2020). Finally, for the hydrological data, we define Q_i to be the dis-295 charge rate at site *i* and v_i to be the average stream velocity between the release loca-296 tion and site *i*. Due to concerns about the measurement precision of stream velocity 297 at each site relative to typical variation over a 1 km stream segment, we set the aver-298 age stream velocity between the release location and each site to the mean of meas-299 ured velocities across sites: $v_i = \bar{v}$. 300

301 4.2 Ecological process model

302 4.2.1 eDNA production, transport, and removal process

We assume site eDNA concentrations are the product of sub-processes for eDNA production, transport, and removal for which we adapt the eDNA Integrating Transport and Hydrology model (eDITH; Carraro et al. 2018), which is a generalization of mass balance models for single eDNA sources (e.g., Sansom and Sassoubre 2017; Altermatt et al. 2023) to multiple sources that accounts for variable hydrology across sites. The eDITH model is:

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$$C_i^{site} = \frac{1}{Q_i} \sum_{j \in \gamma_i} A_j p_{0_j} \exp\left(\frac{-d_{i,j}}{v_{i,j}\tau}\right),\tag{2}$$

where C_i^{site} is the concentration at site *i* (N/m³), where N is the number of eDNA 311 copies, \dot{Q}_i is the water discharge rate at site *i* (m³/s), γ_i is the set of sites upstream of 312 site *i*, A_j is the habitat area of site *j* (m²), p_{0_j} is the eDNA production rate of site *j* (N/ 313 m^2 s), d_{ij} is the distance between site i and j (m), v_{ij} is the mean velocity between 314 site i and j (m/s), and τ is the inverse eDNA removal rate (s). In our experiment, 315 eDNA is added at a point location of zero area, so we remove area and define p_0 to 316 be the eDNA production rate without respect to area with units N/s. Further, eDNA 317 is only "produced" at the release location, removing the need to sum the eDNA con-318 tribution of multiple upstream sites. These modifications simplify the eDITH model 319 to: 320

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$$C_i^{site} = \frac{p_0}{Q_i} \exp\left(\frac{-d_i}{v_i \tau}\right),\tag{3}$$

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where p_0 is the eDNA production rate at the release location, d_i is the distance between site *i* and the release location, and v_i is the mean velocity between site *i* and the release location, which we assume to be constant across sites.

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We consider two versions of the eDITH model above with respect to how eDNA is removed from the water column as a function of time. Note that the expected travel time from the release location to site *i* is $t_i = \frac{d_i}{v_i}$, and the exponential term in the eDITH model is an exponential survival function in continuous time:

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$$S(t) = \exp\left(\frac{-t}{\tau}\right). \tag{4}$$

The removal rate is F(t) = 1 - S(t), and we will use this term for better consist-333 ency with the eDNA literature. Under an exponential model, DNA is removed at the 334 same rate through time. A Weibull model (David and Mitchel 2012; Bylemans et al. 335 2018) considers that the eDNA removal rate can increase or decline through time, 336 but includes an extra parameter, which we found led the eDITH model parameters 337 to be too weakly identified for parameter estimation with our data. A power law 338 relationship (Shogren et al. 2017; Levi et al. 2019) allows the eDNA removal rate to 339 decline through time without an extra parameter; however, (1) if we use a power law 340 relationship as a survival function, $S(t) = t^{-\alpha}$, survival goes to infinity when t is less 341 than 1 and (2) without the scale parameter τ , the time units do not cancel. Therefore, 342 we define $T_i = 1 + t_i$, where T is a non-dimensional time factor, and the survival 343 function as a function of T is: 344

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$$S(T) = T^{-\alpha}.$$
(5)

This survival function is not derived from a distribution for failure times, such as the exponential or Weibull; however, it may still be empirically adequate to describe faster than exponential decay in our experiment.

The resulting eDITH model with power law eDNA removal in continuous time is then:

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 $C_i^{\text{site}} = \frac{p_0}{Q_i} \left(1 + \frac{d_i}{v_i} \right)^{-\alpha} \tag{6}$

for sites 2, ...,13. For both eDITH removal models, we add a thinning parameter at the first site to account for the "plume effect" seen in previous studies (Wood et al. 2020, 2021; Laporte et al. 2020, see Discussion), which describes the phenomenon of delayed mixing with distance from the eDNA source. For example, in the power law version:

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$$C_1^{site} = \theta^{site} \frac{p_0}{Q_1} \left(1 + \frac{d_1}{v_1} \right)^{-\alpha},\tag{7}$$

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where $0 < \theta^{site} < 1$. As a consequence, copy number measurements from site 1 do not contribute to the estimation of the eDITH model parameters beyond ensuring that the concentration at site 2 is greater than or equal to that at site 1.

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364 4.2.2 Sampling process

The sampling process describes the variation in sample concentrations collected at a site as a function of the site concentration. This distribution is typically right-skewed due to eDNA clumping in the water column and stochastic collection of more rare, larger "aggregate" particles (Furlan et al. 2016; Yates et al. 2023); therefore, we use a log-normal distribution (Carraro et al. 2018; Espe et al. 2022) to describe this variation. Conditional on the eDNA concentration at site *i*, we assume that the concentration in each collected sample, C_{ii}^{samp} , varies following:

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$$\log\left(C_{i,j}^{samp}\right) \sim \operatorname{Normal}\left(\log\left(C_{i}^{site}\right), \sigma^{samp}\right),\tag{8}$$

where σ^{samp} is the sampling process standard deviation on the log scale, which could be a function of site covariates such as the distance from the release location.

376 4.2.3 Replication process

The replication process describes the variability in the number of copies allocated to each replicate given the sample concentration. We model the eDNA copy number in each replicate, $N_{i,j,k}$, as a count random variable with an expected number of copies being a function of the sample concentration (Dorazio and Hunter 2015; Furlan et al. 2016). More specifically,

 $\lambda_{ij}^{rep} = C_{ij}^{samp} V_{ij}^{rep},\tag{9}$

where $\lambda_{i,j}^{rep}$ is the expected number of copies in a replicate from site *i* and sample *j* 384 and $V_{i,i}^{rep}$ is the sample volume in cubic meters associated with 1 replicate from site *i* 385 and sample j. If this volume varies across replicates of the same sample, a replicate 386 dimension can be added to λ and V^{rep} . Next, we assume that the eDNA copies are 387 homogeneously distributed throughout the eDNA extract and deposited into each 388 replicate following a Poisson distribution, which has theoretical support for both 389 digital PCR (dPCR) and qPCR (Dube et al. 2008; Rossmanith and Wagner 2011; 390 Tellinghuisen 2020; Lesperance et al. 2021): 391

$$N_{i,j,k} \sim \text{Poisson}\left(\lambda_{i,j}^{rep}\right).$$
 (10)

393

394 4.3 Observation model

The observation model describes both the detection and quantification processes. For the detection process, we assume replicate-level detection probability, $p_{i,j,k}^{y}$, is a function of the number of copies in a replicate:

$$\operatorname{logit}\left(p_{i,j,k}^{y}\right) = \gamma_{0} + \gamma_{1}(N_{i,j,k} - 1).$$
(11)

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By subtracting 1 from the number of copies in each replicate, γ_0 corresponds to the detection probability of 1 copy, and we constrain $\gamma_1 > 0$ with a truncated prior (see Supplementary Materials B). Then, we assume

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$$\left[y_{i,j,k}^{det}|N_{i,j,k}\right] \sim \text{Bernoulli}\left(p_{i,j,k}^{y}N_{i,j,k}^{1}\right),\tag{12}$$

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where $N_{i,j,k}^1 = I_{N_{i,j,k}>0}$ is an indicator variable that zeroes out the detection probability when 0 copies are allocated to a replicate on the logit scale.

Finally, the quantification process, conditioned on detection and the number of copies in a replicate, is

$$\left[\log(y_{i,j,k})|N_{i,j,k}, y_{i,j,k}^{det} = 1\right] \sim \operatorname{Normal}\left(\log(N_{i,j,k}), \sigma^{rep}\right),\tag{13}$$

where $y_{i,j,k}$ is the measured replicate copy number and σ^{rep} is the replicate-level copy number measurement error on the log scale, which could be a function of site, sample, or replicate covariates. Because (1) we condition the quantification process on positive detections and (2) copy number measurements may be censored from below by η_q (Espe et al. 2022), the observed replicate-level quantitative data, $y_{i,k}^{obs}$, are:

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$$\begin{bmatrix} y_{i,j,k}^{obs} | y_{i,j,k}^{det}, y_{i,j,k} \end{bmatrix} = \begin{cases} 0, & \text{if } y_{i,j,k}^{det} = 0, \\ 0, & \text{if } y_{i,j,k}^{det} = 1 \text{ and } y_{i,j,k} < \eta^q, \\ y_{i,j,k}, & \text{if } y_{i,j,k}^{det} = 1 \text{ and } y_{i,j,k} > \eta^q. \end{cases}$$

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This model is depicted in Fig. 1. An important assumption in this quantification 419 process model is that the log copy number measurements are unbiased, i.e., 420 $E[\log(y_{iik})] = \log(N_{iik})$, which can be violated, for example, by a concentration 421 plateau effect (Hunter et al. 2017) or by DNA inhibitors (McKee et al. 2015; Hunter 422 et al. 2019; Sepulveda et al. 2020). We consider the latter in the next section. A final 423 note we will make here is that by conditioning measurement on detection when 424 detection is a function of concentration accounts for the fact that the expected value 425 of measurements for the detected replicates of low concentration samples is larger 426 than $\log(\lambda_{ii}^{rep})$ because the replicates that are allocated the lowest positive copy num-427 bers are less likely to be detected and thus measureable, and replicates that are allo-428 cated 0 copies never produce a quantitative measurement. 429

430 4.4 Extended process model: copy inhibition

Here, we consider that the PCR reaction in each replicate may be partially or completely inhibited, which can decrease both the detection probability and the number of copies measured given detection. Compounds found in the environment can inhibit PCR reactions via multiple mechanisms, including binding to the target DNA and binding to or otherwise interfering with reaction products (Opel et al. 2010; McKee et al. 2015). Inhibition is typically identified by comparing

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Fig. 1 Model diagram for the exponential removal model without an inhibitor processes. The eDITH process describes how concentration is distributed across sites, the sampling process describes how concentration is distributed across samples at a site, the replication process determines how many copies are allocated to each replicate for each sample, the detection process describes how copies in each replicate are detected, and the quantification process describes how detected copies are measured

the *Cq* values of IPCs to uninhibited control samples (Volkmann et al. 2007; Jane et al. 2015, see Lab Methods: Inhibition Assessment) and using a deterministic decision rule to exclude samples likely to be inhibited (e.g., samples with a $\Delta Cq \ge 3$ Goldberg et al. 2016), though others have treated ΔCq as continuous measures of inhibition (Volkmann et al. 2007; Lance and Guan 2020). We take the latter approach, modeling the probability of inhibition as a function of replicate copy number, replicate ΔCq , and a sample-level random effect.

444 For each replicate, the probability of inhibition is $p_{i,ik}^w$, where

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$$\operatorname{logit}\left(p_{i,j,k}^{w}\right) = \beta_0 + \beta_1(N_{i,j,k} - 1) + \beta_2 \operatorname{shift}_{i,j,k} + \sigma^{w} \epsilon_{i,j}.$$
 (14)

shift_{*i,i,k*} is the standardized ΔCq covariate, and $\epsilon_{i,i} \sim \text{Normal}(0, 1)$ (non-centered 447 sample-level random effects; Papaspiliopoulos et al. 2007). Note, we expect the 448 $\beta_1 < 0$ and constrain it to be less than zero with a truncated prior (see Supplemen-449 tary Materials B). The sample random effects account for sample-level heterogeneity 450 in replication inhibition probability, due, at least in part, to sample-level variability 451 in inhibitor concentration. Next, we assume replicate inhibition states are Bernoulli 452 random variables 453

454 455

$$w_{i,j,k} \sim \text{Bernoulli}\left(p_{i,j,k}^{w}\right),$$
 (15)

with $w_{i,j,k}$ taking value 1 when inhibited and 0 otherwise. If a replicate is inhibited, we assume the copies available to be detected and measured, $N_{i,j,k}^{thin}$, result from a 456 457 thinning process of the true copy number: 458

459
$$\left[N_{i,j,k}^{thin}|N_{i,j,k}\right] \sim \operatorname{Binomial}\left(\theta_{i,j,k}^{thin}, N_{i,j,k}\right), \tag{16}$$

where $\theta_{i,j,k}^{thin}$ is the thinning rate, which could be a function of covariates or random 461 effects. For simplicity, we assume $logit(\theta_{i,j,k}^{thin}) = \theta_0$. Then, to determine how many 462 copies are available for detection and measurement as a function of the replicate 463 inhibition states, we specify 464

465 466

$$N_{i,j,k}^{avail} = (1 - w_{i,j,k})N_{i,j,k} + w_{i,j,k}N_{i,j,k}^{thin}$$
(17)

which evaluates to $N_{i,j,k}^{thin}$ if a replicate is inhibited and $N_{i,j,k}$ otherwise. Finally, we replace $N_{i,j,k}$ with $N_{i,j,k}^{avail}$ in the observation model so that detection and measurement 467 468 469 are both conditioned on the inhibition states:

$$\operatorname{logit}(p_{i,j,k}^{y}) = \gamma_0 + \gamma_1 (N_{i,j,k}^{avail} - 1), \tag{18}$$

470 471

472
$$\left[\log(y_{i,j,k})|N_{i,j,k}^{avail}\right] \sim \operatorname{Normal}\left(\log\left(N_{i,j,k}^{avail}\right), \sigma^{rep}\right).$$
(19)

Then, the detection model is the same as Eq. (12), except we redefine $N_{i,i,k}^1 = I_{N_{i,i,k}^{avail} > 0}$, 474 a function of the available copy number instead of the true copy number. 475

The number of copies available to be detected can be interpreted as the number 476 of copies that inhibitors did not bind to, the number of copies measureable given the 477 478 magnitude of binding of inhibitors to polymerase in a replicate, or a combination of both factors. More generally, the main feature of the inhibitor model is a large 479 reduction in the detection probability and measured copy number for inhibited sam-480 ples, which happens regardless of the precise mechanism (Opel et al. 2010; McKee 481 et al. 2015). This extended model is depicted in Supplementary Fig. S1. With this 482 483 model structure, if a replicate is inhibited, its detection probability and expected log copy number measurement given detection both decrease, with detection probability 484

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decreasing to 0 if no copies are available to be detected. Note that the inhibition states, $w_{i,j,k}$, are not directly observed—we can only observe the effects of inhibition on the copy number detections and measurements. However; the specification of our inhibitor model as part of a larger hierarchical model (Royle and Dorazio 2008) allows the inhibition states to be estimated jointly along with the other model variables and latent states.

491 **4.5 Parameter estimation**

We estimated our model parameters using Markov chain Monte Carlo (MCMC) 492 in the Nimble software (Version 1.0.1; de Valpine et al. 2017) in program R (Ver-493 sion 4.0.5; R Core Team 2021). We used Nimble defaults for all MCMC sampler 494 assignments, with some exceptions, specifically, (1) for the inhibitor models, we 495 added user-defined samplers that were required to adequately sample the posterior 496 (described in Supplementary Materials B), (2) due to strong posterior correlation, 497 we used a separate block Metropolis-Hastings updates (Ponisio et al. 2020) for pro-498 cess parameters p_0 , θ^{site} , τ or α , detection parameters γ_0 and γ_1 , and inhibitor param-499 eters β_0^w and β_1^w . Our priors can be found in Supplementary Materials B. 500

501 4.6 Data analysis

502 4.6.1 Model comparisons

To investigate the evidence for and effects of both a non-constant eDNA removal rate with respect to time and eDNA inhibitors, we fit four models:

- Model I–PL—accounts for inhibitors, power law removal,
- Model I–E—accounts for inhibitors, exponential removal,
- Model N–PL—ignores inhibitors (null), power law removal,
- Model N–E—ignores inhibitors (null), exponential removal.

509 While the following are not completely conclusive on their own, we suggest that evi-510 dence supporting the inhibitor models would be (1) a strong lack of fit when ignor-511 ing inhibitors that is reduced when they are modeled (e.g., Model N–PL vs. Model 512 I–PL), (2) a clear negative relationship between the probability of replicate-level 513 undermeasurement events (hypothesized to be caused by inhibition) and the number 514 of copies in a replicate, and (3) a positive relationship between the probability of 515 replicate-level undermeasurement events and the replicate ΔCq .

If the inhibitor models are a good approximation of reality, we expected (by logical implications of the model structure) that when ignoring inhibitors, we would (1) underestimate site concentrations, with larger underestimation as site concentration decreases, (2) overestimate the eDNA removal rate due to under-measuring more at lower concentration sites farther from the source, (3) overestimate both the sampling and measurement variability which must accommodate the effects of inhibition, and (4) underestimate the effect of replicate copy number on detection probability

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because the copy number in each replicate will be underestimated, on average. To compare the inhibitor models to the null models, we used posterior predictive checks (Gelman et al. 1996; Conn et al. 2018) and the conditional Watanabe–Akaike Information Criterion (WAIC; Watanabe and Opper 2010; Gelman et al. 2014). For the posterior predictive check, we used the observation model deviance as the discrepancy function (King et al. 2009; Conn et al. 2018). For the null models, the observation model deviance is

$$T(\mathbf{y}^{obs}, \mathbf{y}^{det}, N, \sigma^{rep}, \gamma_0, \gamma_1) = -2\log\left([\mathbf{y}^{obs}|\mathbf{y}^{det}, \sigma^{rep}, N][\mathbf{y}^{det}|\gamma_0, \gamma_1, N]\right).$$
(20)

The observation model deviance for the inhibitor model is the same as for the null models, except we replace N with N^{avail} . For each data point, we computed the Bayesian P-value, the probability each observed data point's discrepancy is more extreme than that of data simulated from the posterior. We considered observations with Bayesian P-values less than 0.05 to be poorly explained by the model and assumed models with more extreme data were less supported.

To compare inhibitor models via WAIC, we used the conditional WAIC (cWAIC) 538 that considers the observation model likelihood conditioned on the number of cop-539 ies allocated to each replicate, $[y^{obs}|y^{det}, \sigma^{rep}, N][y^{det}|\gamma_0, \gamma_1, N]$. We also used WAIC 540 to compare the removal models; however, cWAIC was not a useful criterion for the 541 process model. In theory, the cWAIC may allow us to compare the exponential and 542 power law process models for these 78 samples (not population-level inference). 543 However, the sample concentrations estimated by these two models were nearly 544 identical (see Results) because the sampling variation was large relative to variation 545 in the observation model, yielding very little shrinkage of sample means toward the 546 site means (for a discussion of shrinkage see Gelman et al. 2013), and thus nearly 547 equivalent conditional likelihoods and WAICs. 548

While the likelihoods conditioned on the latent variables were nearly identical, 549 the process model likelihood for the distribution of sample means around site means 550 on the log scale, e.g., $[\log(C^{samp})|p_0, \tau, \theta^{site}]$ in the exponential removal model, were 551 not. In this case, marginal WAIC (mWAIC) that also considers the process model 552 likelihood is generally more appropriate for process model selection, and further, 553 it considers the ability of models to predict measurements for new clusters (Mer-554 kle et al. 2019; Ariyo et al. 2020, 2022), which here are samples, instead of the 78 555 samples we did measure (population-level inference). For the exponential model, the 556 marginal likelihood is $[\mathbf{y}^{obs}|\mathbf{y}^{det}, \sigma^{rep}, p_0, \tau, \theta^{site}][\mathbf{y}^{det}|\gamma_0, \gamma_1, p_0, \tau, \theta^{site}]$. With continu-557 ous random effects as we have for the sample concentrations, the marginal likeli-558 hood needs to be approximated, for example, with importance sampling, which can 559 be computationally costly (Tran et al. 2021). Further, in our model, to approximate 560 this marginal likelihood, we must first integrate out N^{rep} , which requires summing 561 over large ranges of integers for every replicate. 562

For the null models, we were unable to both integrate out N^{rep} and approximate the marginal likelihood in a reasonable amount of time, and for the inhibitor models, we were unable to integrate out N^{rep} in a reasonable amount of time. Therefore, we instead computed sample-level WAIC using the process model likelihood and the posterior modes of the sample log concentrations from the full exponential

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release models as data, $[\log(\hat{C}^{samp})|p_0, \tau]$. Note, we removed θ^{site} from the marginal 568 likelihood here since we used it to compute the sample log concentrations at the 569 first site to reflect what they were before thinning. We chose to use the sample log 570 concentration point estimates from the exponential model because (1) to compare 571 WAIC, the observed data must be the same, and (2) choosing the exponential esti-572 mates a priori favors the exponential model to the degree the sample concentrations 573 are shrunk toward the exponential process model site means. In sum, we pragmati-574 cally compared the release models evaluated at our best estimates of the sample con-575 centrations. This approach ignores uncertainty in the sample concentrations, but is 576 arguably more reliable than the common practice of averaging technical replicates 577 to obtain sample concentrations to then use as data and compare models due to the 578 challenges of computing sample means outlined in the Introduction. 579

580 4.6.2 Independent eDNA production rate estimate

While the eDNA production rate, p_0 , in our experiment was unknown, we used three 581 samples collected from the cooler from which water was released within 15 min 582 of completing the field sample collection and an estimate of the release rate from 583 the cooler (220 mL/min) to produce independent estimates of p_0 . Because we could 584 not estimate all the sampling, replication, and observation process parameters with 585 only three samples, and the measured replicate copy numbers from cooler samples 586 were large (5.8-8.4 million), we used a simplified estimation approach. We first esti-587 mated the sample log concentrations by averaging the replicate concentrations on 588 the log scale and then used these averages as our three data points. Then, because 589 three data points were not sufficient to estimate the sampling standard deviation with 590 acceptable precision, we did a sensitivity analysis where we estimated p_0 from the 591 cooler samples assuming σ^{samp} was 0.25, 0.5, 1.0, or 1.5, where 0.25 and 0.5 were 592 lower than what we estimated from the inhibitor release models and 1.5 was higher. 593 We then compared the visual overlap in the posterior distributions of p_0 from the 594 four release models to these hypothetical sampling standard deviations for the cooler 595 models. 596

597 4.6.3 MCMC details

For each of the 4 release models, we ran 3 MCMC chains for 300,000 iterations 598 each, with model parameters and latent variables thinned by 25 and 250 iterations, 599 respectively. We discarded 25,000 pre-thinned iterations and assessed convergence 600 using the Gelman-Rubin Statistic (Brooks and Gelman 1998) ensuring the 95% CI 601 upper bound was less than 1.1 for all parameters. Posterior modes were used as point 602 estimates and 95% highest posterior density (HPD) intervals were used as interval 603 estimates. Because the posteriors for N, N^{thin} , N^{avail} , and C^{sample} were often mul-604 timodal in the inhibitor models, we used the HDinterval R package (Meredith and 605 Kruschke 2020) to produce discontinuous HPD intervals. For each of the cooler 606 models (each level of σ^{samp}), we ran 1 chain for 25,000 iterations, discarding the first 607 5000 iterations. 608

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609 4.7 Simulation study

We conducted a simulation study to characterize how well parameters of each model 610 were estimated in terms of percent relative bias (absolute bias divided by the true 611 parameter value and then multiplied by 100), 95% coverage (proportion of data sets 612 for which the 95% HPD covers the true parameter value), and the coefficient of var-613 iation (CV; posterior standard deviation divided by posterior mode multiplied by 614 100) when using data similar to ours in terms of the data dimensions, hydrology, 615 and parameter values. We simulated 100 data sets from each of four models using 616 the parameter estimates from the field data, with the same number of sites, site dis-617 tances, replicate number, and hydrological parameters. The simulation scenarios dif-618 fered from the field data models in two ways—we excluded the thinning process at 619 the first site due to the "plume effect" to assess how well the eDNA production rate, 620 p_0 , can be estimated when ignoring this nuisance parameter, and we excluded the 621 ΔCq covariate as it may not always be available. 622

For each simulated data set from the null and inhibitor models, we ran 3 MCMC 623 chains for 150,000 and 300,000 iterations, respectively, and thinned posteriors by 25 624 to reduce file sizes. For null and inhibitor models, we discarded a minimum burn in 625 of 5000 and 35,000 pre-thinned iterations, respectively. After discarding this burn 626 in, we computed the Gelman–Rubin statistic (\hat{R} ; Gelman and Rubin 1992) for each 627 parameter, ensuring that the 95% confidence interval upper bound of the statistic 628 was below 1.1. For posteriors with \hat{R} 95% confidence intervals greater than 1.1 for 629 any parameter, we discarded more burn in after visual inspection to meet this condi-630 tion. For point estimates, we used the posterior mode, and for interval estimates, we 631 used the 95% HPD interval. For each data set, we computed the CV for all param-632 eters by dividing the posterior standard deviation by the absolute value of the pos-633 terior mode and multiplying by 100. We report the CV averaged across data sets for 634 each model. One exception was for β_0^w , which had point estimates very close to zero, 635 leading to large CVs which were not informative of parameter precision (Kvålseth 636 2017). For this parameter, we computed the CV as the averaged standard deviation 637 divided by the averaged posterior mode multiplied by 100. 638

639 **5 Results**

640 5.1 Observed data and inhibition assessment

We observed no amplification in negative controls or in samples collected upstream of the introduction point and positive controls amplified as expected. The replicatelevel quantitative data ranged from 2.22 to 5.91 \log_{10} copies/L and 0.22–3.91 \log_{10} copies per reaction (Supplementary Fig. S2a). We observed 24 replicates (out of 390) that failed to detect eDNA, with 1, 5, 7, 1, 2 and 8 failed detections at distances of 0.5, 40, 300, 400, 500, and 1000 m, respectively. Three samples failed to detect eDNA across all five replicates, one sample each at distances of 40, 300, and 1000

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m. Our inhibition assessment did not indicate inhibition for any replicates using the decision rule of $\Delta Cq \geq 3$. Shifts in Cq ranged from -0.13 to 1.60 with a mean of 0.11 cycles. The distribution of ΔCq was right skewed, with most values clustered slightly above zero (Supplementary Fig. S2b).

652 5.2 Analysis of field data

The four models we considered produced substantially different parameter estimates, 653 leading to different inferences about the ecological and observational processes that 654 produced our data (Table 1). The inhibitor models estimated that the sampling pro-655 cess standard deviation, σ^{samp} was smaller and the quantification process standard 656 deviation, σ^{rep} was larger, compared to the null models. The inhibitor models further 657 estimated that the removal rate (governed by α or τ) was lower compared to the null 658 models, and that site concentrations were higher, particularly at the sites farthest 659 from the source (Fig. 2). 660

The power law removal models estimated the eDNA production rate at the source to be much larger than the exponential removal models (Fig. 3) and correspondingly, estimated the percent of total concentration that is measurable at the first site, θ^{site} to be lower (Table 1). Finally, the effect size of replicate copy number on replicate detection probability was estimated to be greater in the inhibitor models relative to the null models.

The Bayesian P-values from the deviance discrepancy function identified 14 sam-667 ples as having replicates that were more extreme than expected under both versions 668 of the null models (Table 2). These samples were characterized by having lower 669 copy numbers, with one or more replicate measurements being much larger than the 670 others, and they disproportionately came from the sites with the lowest measurable 671 concentrations (first site with plume effect and sites farthest from the source). For 672 the inhibitor models, the Bayesian P-values identified four samples having replicate 673 measurements that were more extreme than expected by the model. The replicates of 674 these samples were also imbalanced but to a lesser or greater degree than expected 675 compared to our thinning rate estimate, $inv.logit(\theta_0) = 0.09$, suggesting heterogene-676 ity in the sample-level thinning rate. WAIC favored the inhibitor models over the 677 null models, with the increased number of effective parameters outweighed by the 678 substantially higher log posterior predictive density (Table 3). 679

Our WAIC estimates using the likelihood for sample log concentrations (Table 3) 680 favored the power law model over the exponential model by 28.27 and 37.46 units 681 when considering and not considering inhibition, respectively. The similarity of the 682 posterior modes for log sample concentrations between removal models can be visu-683 alized in Supplementary Fig. S3, where estimates from the null models are nearly 684 identical between exponential and power law removal, and estimates from the inhib-685 itor models were nearly identical except for 2-3 data points. We provide this infor-686 mation to justify using the posterior modes of sample log concentrations from the 687 exponential model as data to evaluate the relative support for each release model, 688 and reiterate that doing so a priori favors the exponential model to the extent that the 689 posterior modes for log sample concentrations differ between removal models. Our 690

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Fig. 2 Posterior point and interval estimates of site and sample concentration as a function of distance for all four models. Note, some 95% HPD intervals are discontinuous due to multimodal posterior distributions. Estimates from Models I–PL and I–E accounting for inhibitors are generally higher, and to a greater magnitude as distance increases. Estimates from Models I–PL and N–PL are higher at sites 2–4 compared to Models I–PL and N–PL, respectively, due to an increasing removal rate through time

second line of evidence to discriminate between removal models is the comparison of the posteriors for the eDNA production rate, p_0 , between the release and cooler models (Fig. 4). While we do not know what the sampling standard deviation, σ^{samp} , was in the cooler, the p_0 estimates from all cooler models overlap more with the power law release models, particularly when inhibition is considered. Our point estimate for σ^{samp} was 0.15; however, this estimate is unlikely to be accurate with only 3 samples.

Parameter estimates with posterior standard deviations and 95% HPD intervals for Model I–PL can be found in Table 4. Model I–PL estimated that many replicates in the range of $1.5-2.5 \log_{10}$ copies were substantially undermeasured, but after accounting for the inhibition process, the copies available to be measured

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eDNA Survival Function

Fig. 3 Survival functions from Models I–PL and I–E, with power law and exponential survival, respectively. Under the power law model, there is more eDNA estimated to be added at the source location relative to the exponential, and faster removal that slows down through time. The expected time at which eDNA reaches sites 1–6 are indicated on the plots, which were derived from our mean velocity measurement

corresponded well with the measured copy numbers (Fig. 5). In Model I–PL, the probability of inhibition was estimated to be inv.logit($\hat{\beta}_0^w$) = 0.85 for a replicate with 1 copy (and random effect value set to 0), with a negligible probability of inhibition over 300 copies/replicate (Fig. 6). The ΔCq covariate was estimated to be positivelyrelated to the probability of inhibition (Table 4), with a 95% HPD that did not overlap 0 and a posterior probability of being greater than 0 equal to 0.99.

708 5.3 Simulation study A

Our ability to estimate parameters in terms of bias, coverage, and precision (CV) 709 varied across parameters and models, with generally better estimates from null mod-710 els over inhibitor models and exponential over power law removal models (Supple-711 mentary Table S1). For the null models, coverage was roughly nominal (e.g., 95% 712 713 CI covered the true value 95% of the time), but the detection parameters were moderately biased (-7.2 to 24.6%) and estimated imprecisely (CVs of 58.8-133.8%). 714 Further, the null model with exponential removal estimated the eDNA production 715 rate, p_0 with minimal bias (2.8%) and a CV of 29.0%, whereas the estimate from the 716 null power law removal model was positively biased by 5.2%, and less precise (CV 717 of 56.6%). The sampling and measurement standard deviations, σ^{samp} and σ^{rep} , were 718 estimated with minimal bias (< 3%) in the null models. 719

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Fig. 4 Plots of the posterior distributions of the eDNA production rate, p_0 , from the four release models and four cooler models with different hypothetical sampling standard deviations, σ^{samp} (indicated with "SD" on the plot). For release models, "PL" indicates "power law," "E" indicates "exponential," "I" indicates "inhibitor," and "N" indicates "null." More overlap between particular release and cooler models indicates more consistency between the estimates

For the inhibitor models, we saw results similar to the null models. Overall, cov-720 erage was roughly nominal for the inhibitor models with the possible exception of 721 reduced coverage for some parameters in model I-PL (our estimates are subject to 722 some sampling variability with only 100 data sets). The detection parameters were 723 biased (-10.6 to 2.0%) and estimated imprecisely (CVs of 52.9-93.6%). The eDNA 724 production rate, p_0 , was estimated with modest negative bias in Model I–E with 725 exponential removal (-4.6%) and modest positive bias in model I–PL with power 726 law removal (8.6%). The p_0 estimates in the inhibitor models were more precise as 727 judged by the CV, likely due to the larger simulated values used in the inhibitor 728 models leading to larger posterior modes. All parameters determining the probabil-729 ity of inhibition were estimated with bias, particularly the intercept β_0^w , which was 730

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Fig. 5 Comparison of the relationship between measured and true copies in each replicate (left) and measured and available copies in each replicate (right) from Model I–PL accounting for inhibitors. In each plot, the posterior probability of inhibition is indicated by the color of the point estimate and 95% HPD intervals are depicted, some of which are discontinuous due to multimodal posteriors. In the plot on the left, the group of true copies measured too low with poor coverage correspond to the samples to which the model assigns a high posterior probability of inhibition. After accounting for inhibition (plot on right), the relationship between measured and available copies is roughly linear with coverage 0.87



Fig. 6 Plots depicting the effects of copy number and ΔCq on the expected probability of inhibition (posterior mean and 95% HPDs), $p_{i,j,k}^w$, and the posterior probability of inhibition, $P(w_{i,j,k} = 1)$. Replicates from samples with no detections (complete nondetects) are colored red, and replicates without detections in samples where other replicates were detected (partial nondetects) are colored orange. The probability of inhibition declines as a function of replicate copy number, with complete and partial nondetects all being estimated to have very few copies (left). The probability of inhibition increases with ΔCq , particularly for replicates with fewer copies (N = 25 scenario)

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Table 1 Parameter point estimates for all four models	Process	Par	Models			
applied to the field data			I–PL	I–E	N–PL	N–E
	eDITH	p_0	6134.78	419.13	12, 076.28	244.69
	eDITH	α	0.59		0.91	
	eDITH	τ		1431.82		873.94
	eDITH	θ^{site}	0.04	0.34	0.01	0.15
	Sampling	σ^{samp}	0.90	1.20	1.34	1.67
	Replicate Inhibition	β_0^w	1.44	1.46		
	Replicate Inhibition	β_1^w	- 0.02	- 0.02		
	Replicate Inhibition	β_2^w	1.16	1.19		
	Replicate Inhibition	σ^w	3.28	3.44		
	Inhibitor Thinning	θ_0	-2.31	-2.36		
	Detection	γ_0	- 2.52	- 2.41	- 2.31	- 2.25
	Detection	γ_1	2.80	2.79	1.28	1.32
	Quantification	σ^{rep}	0.29	0.29	0.68	0.68

Model I–PL accommodates inhibitors and has power law removal, Model I–E accommodates inhibitors and has exponential removal, Model N–PL does not accommodate inhibitors and has power law removal, Model N–E does not accommodate inhibitors and has exponential removal. p_0 was modeled in m³/s units and presented here in L/s units

negatively biased by 19.7–23.3% in the inhibitor models. As in the null models, the sampling and measurement standard deviations, σ^{samp} and σ^{rep} , were estimated with minimal bias (<3%), except for σ^{samp} in model I–PL with a bias of 5.9%.

734 6 Discussion

We developed a hierarchical model for eDNA fate and transport experiments that 735 accommodates more mechanistic detail about how eDNA is detected and measured 736 than existing models. We also conducted an eDNA release experiment to demon-737 strate the utility of this modeling approach for estimating eDNA removal parameters 738 in the presence of ecological and measurement variability. Two distinctive features 739 of the model are that site concentrations are modeled as the product of an eDNA 740 removal process as a function of time (using the eDITH approach of Carraro et al. 741 2018) and that replicate copy numbers are regarded as latent variables modeled with 742 a count distribution. The latter feature has several advantages for low concentra-743 tion samples and facilitates modeling detection, measurement error, and sources of 744 bias as functions of the ecological quantity being measured—the discrete number 745 of copies in each replicate. Using this model, we were able to provide evidence that 746 the eDNA removal rate in our experiment declined through time (e.g., power law 747 removal) and that the allocation of measurable copies across replicates was overdis-748 persed relative to the Poisson in a subset of samples. We then developed a model for 749

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Table 2 Samples with replicates	M- 1-1	C:4-	C	D 1	D 2	D 2	Dava 4	D 5
where Bayesian P-values from	Model	Site	Sample	Rep I	Rep 2	Rep 3	Rep 4	Rep 5
posterior predictive checks	Null	1	1	2.57	66.33	62.70	3.41	3.86
the P-value being less than 0.05	Null	1	3	0	7.08	4.88	472.19	4.16
	Null	1	6	125.24	71.73	4.75	121.01	5.86
	Null	8	5	62.79	6.35	164.17	11.97	8.67
	Null	10	1	110.24	5.66	9.56	7.31	5.53
	Null	11	3	8.16	74.08	7.98	10.39	141.60
	Null	11	4	68.67	7.37	7.88	11.77	6.02
	Null	11	6	70.95	2.56	3.30	84.97	4.21
	Null	12	1	2.31	7.94	5.57	2.64	52.09
	Null	12	2	8.30	9.61	4.28	66.94	9.94
	Null	12	3	42.74	5.61	0	3.24	2.38
	Null	13	3	2.42	48.81	18.51	1.83	0
	Null	13	4	31.04	3.61	0	87.01	4.80
	Null	13	5	70.73	3.49	5.00	8.21	5.42
	Inhibit	1	3	0	7.08	4.88	472.19	4.16
	Inhibit	1	4	44.27	102.19	38.40	16.92	18.84
	Inhibit	6	4	202.90	54.30	62.58	90.22	77.76
	Inhibit	8	4	67.78	74.98	76.75	291.60	76.44

Samples are listed by model ("Null" and "Inhibit" without and with modeling inhibitors, respectively), site, and sample, along with the observed data for each sample replicate. Null models are N-E and N-PL and inhibitor models are I-E and I-PL

Model	WAIC Target	WAIC	lppd	pWAIC
I-PL	Rep	334.96	- 33.61	133.87
I–E	Rep	333.34	- 33.16	133.51
N-PL	Rep	912.28	- 360.87	95.27
N–E	Rep	913.20	- 360.33	96.27
I–PL	Samp	219.15	- 105.75	3.83
I–E	Samp	256.61	- 124.49	3.82
N-PL	Samp	278.84	- 135.26	4.16
N–E	Samp	307.11	- 149.87	3.69

Two types of WAIC are used, with a WAIC Target of "Rep" being the conditional WAIC at the level of replicates and a WAIC Target of "Samp" being the conditional WAIC at the level of samples. For sample-level WAIC, we were unable to incorporate the uncertainty in the sample concentrations, and the sample-level WAIC values are not directly comparable between the null and inhibitor models, see "Methods"

Table 3 WAIC table showing the WAIC, log posterior predictive density (lppd) and effective number of parameters (pWAIC) for all four models

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Process	Par	Est	SD	Lower	Upper
eDITH	p_0	6134.78	3079.41	2834.56	13, 769.82
eDITH	α	0.59	0.07	0.47	0.74
eDITH	θ^{site}	0.04	0.03	0.01	0.12
Sampling	σ^{samp}	0.90	0.10	0.75	1.13
Replicate Inhibition	β_0^w	1.44	0.98	- 0.24	3.65
Replicate Inhibition	β_1^w	- 0.02	0.01	-0.05	- 0.01
Replicate Inhibition	β_2^w	1.16	0.54	0.20	2.32
Replicate Inhibition	σ^w	3.28	0.77	2.20	5.10
Inhibitor Thinning	θ_0	- 2.31	0.10	- 2.51	- 2.11
Detection	γ_0	- 2.52	1.28	- 5.63	-0.70
Detection	γ_1	2.80	1.78	1.05	6.99
Quantification	σ^{rep}	0.29	0.02	0.26	0.33

Table 4Parameter point and interval estimates and posterior standard deviations from Model I–PL thataccommodates inhibitors and considers power law removal

 p_0 was modeled in m³/s units and presented here in L/s units

how eDNA inhibitors might reduce the measurable copy numbers in the replicates
and show the pattern of overdispersion in our observed data is largely consistent
with this model.

Treating copy numbers in replicates as count random variables provides sev-753 eral advantages when site and sample concentrations are low. To date, quantitative 754 eDNA analyses have typically assumed sample or replicate concentrations are nor-755 mally-distributed, usually on the log scale (Carraro et al. 2018; Espe et al. 2022; 756 Shelton et al. 2019). Our model highlights that replicate-level measurement error 757 is the product of both sampling variation when allocating copies to the replicates 758 (Dube et al. 2008; Lesperance et al. 2021) and the measurement error conditioned 759 on the number of copies in each replicate (due to variation in factors such as read-760 ing fractional cycle numbers; Shelton et al. 2019). An implication of a count model 761 for the replication process is that a normal approximation will be a less appropriate 762 when measuring small copy numbers (Espe et al. 2022) that are typical of many 763 eDNA applications. Then, when sample concentrations are low enough that qPCR 764 replicate-level zeros are observed, it is unknown whether a zero is observed because 765 there were no target DNA copies allocated to a replicate or because the allocated 766 copies were undetected (Dube et al. 2008; Lesperance et al. 2021). To compute an 767 unbiased sample mean concentration in the presence of observed zeros, the replica-768 tion process zeros need to be included, as do the true allocated copy numbers for 769 replicates with failed detections, which are not observed. 770

Techniques that allow a probabilistic interpretation of zeros and non-detections have been recognized as critical by many disciplines, like analytical chemistry and public health (e.g., Chik et al. 2018), and have been used by eDNA practitioners when computing the limit of detection in qPCR (Dube et al. 2008; Lesperance et al. 2021). By conditioning detection on copies being present in replicates, and relating the detection probability to the number of copies in a replicate, our model can

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probabilistically resolve these sources of zeros and produce less biased estimates 777 of replicate copy numbers and sample concentrations in this situation. In practice, 778 the accuracy of the resulting estimates will depend on how well model assumptions 779 are met, and estimates may be very imprecise when samples have concentrations so 780 low that most replicates are true sampling zeros. Further, in Simulation Study A, we 781 show that the detection parameters that are a function of latent copy numbers are 782 weakly identifiable, estimated with low precision and moderate bias. We assume this 783 is due to the magnitude of uncertainty in the estimates of the latent copy numbers 784 near zero, which is greater in the inhibitor models where the bias in the detection 785 probability of one copy is larger. Therefore, the performance of this model in terms 786 of bias and precision of the ecological parameters in scenarios with lower sample 787 concentrations than we observed and/or greater sampling variability should be fur-788 ther investigated. This approach of partitioning variation between the allocation of 789 copies and measurement of copies may also be used in standard curve experiments 790 (e.g., Klymus et al. 2020) to relate Cq to the realized, instead of expected, copy 791 number of standards. Doing so could reduce the nonlinearity seen in standard curve 792 calibration regressions (Klymus et al. 2020) due to observing true and false zeros at 793 low concentration standards. 794

Including latent replicate copy numbers in the model also provides a means for 795 detecting deviations from Poisson variability in the replication process, and explor-796 ing hypotheses about potential causes of this assumption violation. We were able 797 to use posterior predictive checks to identify lack of fit in our null models consist-798 ent with overdispersion in the number of copies allocated to replicates. This over-799 dispersion was only seen in a subset of samples, and appeared stochastic in nature, 800 with replicates tending to show a bimodal pattern of high and low measurements in 801 affected samples. In theory, general overdispersion could result from sample-level 802 variability in measurement error, given the number of copies allocated to each rep-803 licate, but we were unable to devise a measurement error hypothesis that explained 804 sample-level heterogeneity and the apparent bimodality in affected samples. Fur-805 ther, we did not find general overdispersion hypotheses, such as pipetting error, to 806 be plausible because most samples were consistent with Poisson replication process 807 variability. 808

A benefit of our hierarchical modeling approach is that we can construct and 809 evaluate hypotheses for plausible mechanisms of this overdispersion pattern. Using 810 the common decision rule of $\Delta Cq \geq 3$ (e.g., Hartman et al. 2005; McKee et al. 2015; 811 Goldberg et al. 2016), none of our samples would be classified as inhibited (Fig. 812 S2b). However, given the general vulnerability of PCR quantification to inhibition 813 (Opel et al. 2010; Sidstedt et al. 2020), the lack of a standard criterion to describe 814 degrees of inhibition (Lance and Guan 2020), and variation in how different assays 815 respond to the same inhibitor (Lance and Guan 2020), we suspected this decision 816 rule may not be well calibrated for our assays and inhibition may have gone unde-817 tected using this method. We used our extended hierarchical model to evaluate the 818 hypothesis that eDNA inhibitors were reducing detection probability and measured 819 copy numbers in our field data, and these inhibitor effects were stochastic, leading 820 to undermeasurement of some replicates of some samples. In the model, inhibi-821 tors have a continuous effect, causing undermeasurement, then failed detection, 822

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depending both on the starting copy number and the magnitude of the underestimation caused by the inhibitors.

We suggest that the posterior predictive checks provide support for the inhibitor 825 models over the null models. The inhibitor model did not provide a clear indica-826 tion of lack of fit for 13/14 of the poorly explained samples from the null model 827 (Table 2), and the four samples that were identified by the posterior predictive check 828 as indicating lack of fit in the inhibitor model were cases that are consistent with 829 inhibition, but with a thinning rate lower or larger than our estimate of $\theta^{thin} = 0.09$ 830 (assuming binomial variability). This extra-binomial variability could be accommo-831 dated with a sample-level random effect in the inhibitor thinning process, or per-832 haps both the probability and magnitude of inhibition could be related to the same 833 latent variable representing inhibitor concentration in a sample. Conditional WAIC 834 also highly favored the inhibitor model. A second line of evidence for the inhibi-835 tor hypothesis is that the probability of inhibition was positively associated with the 836 ΔCq covariate with a posterior probability $\beta_2^w > 0 = 0.99$. Still, we cannot conclu-837 sively rule out other causes of the overdispersion we saw in our data, and it may 838 result from more than one cause. 839

Hypothetically interpreting our field data in light of the inhibitor model, inhi-840 bition started to occur in the range of 100-400 copies/replicate. As copy number 841 approached zero, between 60 and 100% of the replicates were likely to be inhibited 842 (interpreting 95% CIs in Fig. 6). If inhibitors were as prevalent in our data as our 843 model suggests, this would indicate that exogenous IPC Cq shifts may not always 844 have high statistical power to detect inhibition at magnitudes that substantially affect 845 measurements. Whether the source of overdispersion we detected was due to a 846 mechanism increasing variability or one causing systematic undermeasurement, like 847 inhibitors, is of high importance. The latter will cause us to systematically under-848 estimate site and sample concentrations disproportionately such that as concentra-849 tion declines, the rate of eDNA removal is overestimated and the sampling process 850 variability is inflated (i.e., attributing inhibitor-induced variability to ecological vari-851 ability). Our model provides a framework to compare alternative hypotheses, using 852 either field or experimentally manipulated samples, to such extent that these hypoth-853 eses imply that different data will be observed. A final caveat is that the signal of 854 inhibition is eroded as copy number approaches zero because of the magnitude of 855 measurement error given the available copy number. For the inhibitor model param-856 eters to be identifiable, we require samples with concentrations high enough that the 857 magnitude of imbalance (relative to Poisson sampling variability) across replicates 858 is large relative to measurement error, but not so large that inhibition did not occur. 859 Lower concentration samples are more likely to have all replicates inhibited, so no 860 imbalance is observable. Our simulation results indicate that the probability of inhi-861 bition parameters (β^{w} and σ^{w}) were weakly identifiable for data sets similar to ours, 862 and we expect they will be completely unidentifiable in many cases. 863

By using the eDITH model to describe eDNA removal as a function of time, we were able to provide evidence that the eDNA removal rate was not constant through time. WAIC favored the power law removal model both when we did and did not consider inhibition. Further, the posteriors for p_0 from the power law release model overlapped more with the posteriors for p_0 estimated in the cooler;

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however, our cooler estimates are speculative since we do not know the sampling 869 variation in the cooler. Presumably, the turbidity of the stream could increase 870 the sampling standard deviation and our point estimate of the sampling standard 871 deviation in the cooler was 0.15, much lower than estimated in the release mod-872 els: however, other factors likely need to be considered and the cooler standard 873 deviation was estimated with only three samples. If the power law model is closer 874 to the truth, the eDNA production rate parameter, p_0 , is challenging to estimate 875 given our study design and the magnitude of sampling variance we encountered. 876 In Simulation Study A, we see that p_0 is estimated with negligible bias in the 877 exponential removal models, but moderate positive bias in the power law removal 878 models. Then, the CV is roughly twice as large for the power law removal mod-879 els. We attribute this to the challenge of (1) extrapolating the pattern in observed 880 concentrations back to the source location when concentration is declining rap-881 idly (Fig. 3) and (2) a large sampling standard deviation. We believe these chal-882 lenges also extend to the more appropriate Weibull removal model, where we 883 found that p_0 and the Weibull scale parameter were effectively jointly unidentifi-884 able with our data, but identifiable if we simulated similar data with a far lower 885 sampling standard deviation. Regardless of the true removal model, using the 886 exponential model if the removal rate decreases through time will negatively bias 887 the estimated eDNA production rate at the source, which will be propagated to 888 downstream metrics like site abundance. 889

One factor that introduces some unaccounted for uncertainty to our evidence for 890 a declining removal rate is that we do not know the reason that the concentration 891 at the first site was estimated to be lower than the second site. If the mechanism(s) 892 causing the concentration at the first site to be undermeasured causes the concentra-893 tion at the second site to be overmeasured, this could cause the data to appear to 894 be undergoing a declining rate of removal. Conversely, if this mechanism caused 895 the concentration at sites beyond the first site to also be undermeasured, we would 896 have underestimated the support for the power law removal model over the exponen-897 tial. Our hypothesis is that concentration at the first site was undermeasured because 898 eDNA did not immediately dissolve throughout the water column (Wood et al. 2020, 899 2021), and the bucket we used to collect water to then split into the six samples at 900 the first site disproportionately sampled water where the eDNA concentration was 901 lower than average for that site. Our release mechanism deposited water from the 902 cooler on top of the stream and we expect it took some time for the eDNA to reach 903 lower in the water column due to gravitational settling (Harrison et al. 2019). This 904 effect has been documented along the horizontal dimension in rivers (Wood et al. 905 2020, 2021; Laporte et al. 2020), where it has been termed a "plume effect." We 906 suggest a similar pattern may occur in the vertical dimension when sampling very 907 close to an eDNA source, depending on where in the water column water is sam-908 pled. When we sampled the first site, the water with the highest concentration of 909 eDNA may have flowed over the bucket and we may have disproportionately sam-910 pled water with a lower concentration of eDNA. If this was the mechanism causing 911 underestimation at the first site, we do not believe it would cause overestimation 912 at the second site. Therefore, we suggest that while not conclusive, our study adds 913 to the evidence for the hypothesis that, in the context of a mass-balance model of 914

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eDNA production, transport, and decay, the removal term is large and the transport term is small (Tillotson et al. 2018).

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Finally, we discuss implications of our model and results for applications of the 917 eDITH model to observational data and for occupancy analyses using detection data 918 only. To our knowledge, the eDITH model has only been applied to observational 919 data sets where: (1) the concentration observed at one site is the product of multi-920 ple upstream sites with different eDNA production rates and (2) release locations 921 are estimated because they are not known. In contrast, our study system used a sin-922 gle, known release location. If eDNA decay declines at the rate we estimated, the 923 majority of the total eDNA produced in a river network would be ignored, and the 924 resulting site concentrations would be underestimated. Further, this underestimation 925 would be predominately close to the sources, so measured site concentrations would 926 not be related to true site concentrations by the same proportionality constant across 927 space (inhibition could also cause deviations from a fixed proportionality constant). 928 The assumptions of the eDITH model are hard to scrutinize given the number and 929 magnitude of sources of ecological and measurement variability and the number of 930 parameters and latent variables that must be estimated. We demonstrated how some 931 assumptions can be better tested in more simple experiments and recommend more 932 and better-controlled experiments be conducted in order to better understand the 933 reliability of this approach when applied at large spatial scales. 934

While we developed our model in the context of an eDNA release experiment 935 with a single source, eDNA production at a site can be conditioned on latent occu-936 pancy states. This model can also be used for occupancy-type designs with inde-937 pendent sites, with site concentration conditioned on latent occupancy states. 938 A principal implication of our model for natural resource management is that for 939 occupancy analyses, site, sample, and replicate variability in concentration and copy 940 number induce detection heterogeneity at all three of these levels. If this variabil-941 ity is not modeled using either observed covariates or random effects, ecological 942 inference may be unreliable. Perhaps the most important effect is that if (1) sites 943 vary in concentration and (2) at least some site concentrations are low enough to 944 lead to missed detections, there will be site heterogeneity in detection probability 945 and subsequent underestimation of the occupancy probability, and thus the potential 946 for misguided natural resource decision making (Royle and Nichols 2003). Also of 947 importance is that the reliability of inference from false positive occupancy mod-948 els depends on how well heterogeneity in true positive detection is accounted for 949 (McClintock et al. 2010; Ferguson et al. 2015). 950

Replacing our eDITH process with processes for independent site occupancy and 951 concentration conditioned on site occupancy would allow for the occupancy states 952 and concentrations at unmeasured sites to be jointly estimated. A caveat, though, 953 is that the reliability of the concentration estimates at sites with no detections (dis-954 proportionately those with the lowest concentrations) will likely depend on the 955 adequacy of the distribution used to model site concentration variability (e.g., log-956 normal variability in site concentration). Further, the performance of such a model 957 will depend on the abundance and reliability of copy number data. Even if not used 958 in practice for occupancy analyses, our model can be used to assess how reliable 959 ecological inference is in the presence of these forms of detection heterogeneity. 960

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961 Ultimately, biostatistical approaches such as those presented in this study help 962 resolve uncertainties associated with eDNA fate and transport as well as qPCR 963 detection and measurement of scarce molecules. Implementation of these types of 964 approaches is needed to more fully take advantage of the potential for eDNA analy-965 sis to contribute natural resource management (Kelly et al. 2023).

966 Appendix: Lab methods and selected results

967 Methods: assay development

Assays designed for eDNA studies using qPCR generally target short amplicons that 968 are between 50 and 150 base pairs (bp) in length (Goldberg et al. 2016; Rees et al. 969 2014) because PCR efficiencies are higher for shorter amplicons (Bustin and Hugget 970 2017) and because shorter DNA fragments tend to be more available for detection in 971 aquatic environments than longer fragments (Bylemans et al. 2018). To explore dif-972 ferences in transport dynamics of short and long DNA fragments, two probe-based 973 qPCR assays were developed for use in this study. Both assays target the T. arcticus 974 cytochrome oxidase subunit 1 gene (cox1) and share the same reverse primer. The 975 first unique set of forward primer and positive-sense strand probe produces a 128 bp 976 amplicon while the second set produces a 468 bp amplicon. In silico validation was 977 performed by aligning all available T. arcticus cox1 gene from NCBI and BOLD 978 databases and identifying conserved regions of DNA greater than 15 base pairs in 979 length. We then used NCBI's nucleotide BLAST to remove areas with high similar-980 ity to any off-target sequences. The primer sequences that were selected with the 981 appropriate thermal properties minimized similarity with sequences outside of the 982 Thymallus genus. The only teleost fish (outside of the Thymallus genus) with fewer 983 than three base pair mismatches with at least one primer was Liopropoma olnevi, 984 a Caribbean reef fish. NCBI Primer-BLAST was used to confirm this result in the 985 nucleotide (nr) database of teleost fishes using default stringency and specificity set-986 tings. Notably, while the assays designed here can reliably detect T. arcticus, there 987 is also significant sequence similarity with other members of the *Thymallus* genus. 988 Therefore, these assays should not be considered species specific when used in water 989 bodies that may contain other members of Thymallus. 990

Each assay's annealing temperature was optimized using temperature-gradient 991 qPCR (from 58 to 67 °C), wherein the optimal annealing temperature was that which 992 minimized the Cq when amplifying replicate synthetic DNA standards of 5000 gene 993 copies. The optimal primer ratios were determined similar to Wilcox et al. (2015). 994 The limit of detection (LOD) and limit of quantification (LOQ) were determined in 995 both an ideal sample matrix (i.e., molecular grade water) and in a relevant sample 996 matrix (extracted water from the study creek) using the eLowQuant method of Les-997 perance et al. (2021). 998

The assays were validated in vitro with DNA extracted from *T. arcticus* from the study creek and from tissues of regional origin of *Salvelinus fontinalis*, which do occur in our study reach, and other salmonids found in nearby waters including *Oncorhynchus mykiss*, *O. clarkii bouvieri*, *O. clarkii lewisi*, *Salmo trutta*, and

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Prosopium williamsoni. Tissue validation was performed with 10 replicates each.
 In situ validation was performed on eDNA water samples collected from the brood
 stock reservoir (known positive source) and from the study creek water collected
 above the barrier prior to the start of the experiment (known negative source).

1007 **Results: assay comparison**

We observed substantially higher detection and copy number measurements using 1008 the short amplicon compared to the long amplicon assay. For the long amplicon 1009 assay, 37.5% of replicates were nondetections and 32.1% of samples failed to detect 1010 eDNA across all 5 replicates, compared to 6.2 and 3.8%, respectively, for the short 1011 amplicon assay. The short amplicon replicate-level quantitative data ranged from 1012 1.71 to 4.90 \log_{10} copies/L and -0.29 to 2.90 \log_{10} copies/reaction and the long 1013 amplicon replicate-level quantitative data ranged from 2.22 to 5.91 log₁₀ copies/L 1014 and 0.22 to 3.91 \log_{10} copies/reaction. Due to the poorer performance of the long 1015 amplicon assay, we used the short amplicon assay data for analysis. 1016

1017 Methods: DNA extraction

1018 All eDNA and tissue samples were extracted with Qiagen DNeasy Blood and Tis-1019 sue Kits (cat. #69504) with Qiagen DNeasy Lyse and Spin Baskets (cat. #19598) 1020 with minimal alterations of the manufacturer's protocol. DNA was eluted in 400 μ L 1021 of Qiagen Buffer AE. All DNA extraction batches included an extraction negative 1022 control using only extraction kit reagents. These extraction blanks were otherwise 1023 handled and analyzed identically to samples.

1024 Methods: quantitative PCR

Assays were run on a BioRad CFX 96-Touch or BioRad Opus thermal cycler (Her-1025 cules, CA). Reactions took place in BioRad Hard-Shell®optical 96-well plates (cat. 1026 #HSP9601) sealed with BioRad Microseal®optical adhesive film (cat. #MSC1001). 1027 The thermal cycle was: 95 °C for 15 min then 50 cycles of 94 °C for 15 s and 60 1028 $^{\circ}$ C for 60 s. Reactions of 20 µL included 10 µL of Qiagen Quantitect Master Mix, 3 1029 µL sterile water, 0.5 µM of forward and 0.4 µM of reverse primer, 0.25 µM FAM-1030 labeled hydrolysis probe, and 4 µL of DNA extract. The two T. arcticus assays were 1031 not multiplexed together, but were run in separate reactions multiplexed with an 1032 internal positive control (IPC, see below). Every 96-well plate run as part of this 1033 study had the same duplicated (two replicates) controls: six point 1:10 dilution T. 1034 arcticus synthetic standard curve ranging from 4e0 to 4e5 target DNA copies, no-1035 template control (NTC), and internally blocked negative control (IBC). FAM and 1036 VIC fluorescence values were ROX-normalized prior to baseline correction and 1037 amplification detection (Patrone et al. 2020) using R v4.0.3 statistical software (R 1038 Core Team 2021). Successful amplification of DNA was defined as any curve for 1039 which a feasible solution with less than 10% transformation error was found for the 1040 non-linear optimization transformation presented in Patrone et al. (2020). 1041

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Author contributions AS and PH conceived and designed the experiment. BA led model development, data analysis, and the writing of the manuscript. PH and AS contributed to model development and data analysis. PH performed all laboratory analyses. All authors contributed to data collection and writing the manuscript.

1058 **Declarations**

- 1059 Conflict of interest We have no conflicts of interest to report.
- Open research statement Data and code are provided at: https://datadryad.org/stash/share/YSe7cJkr8w
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